



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE/
*NASIONALE
SENIOR SERTIFIKAAT***

GRADE/GRAAD 12

SEPTEMBER 2018

**MATHEMATICS P1/WISKUNDE V1
MARKING GUIDELINE/NASIENRIGLYN**

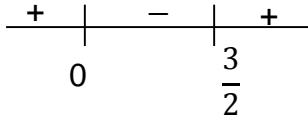
MARKS/PUNTE: 150

This marking guideline consists of 12 pages./
Hierdie nasienriglyn bestaan uit 12 bladsye.

NOTE/LET WEL:

- If a candidate answers a question TWICE, mark the FIRST attempt ONLY.
Indien 'n kandidaat 'n vraag TWEE keer beantwoord, merk SLEGS die EERSTE poging.
- Consistent accuracy applies in ALL aspects of the marking guideline.
Volgehoue akkuraatheid geld deurgaans in ALLE aspekte van die nasienriglyn.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
Indien 'n kandidaat 'n poging vir 'n vraag deurgetrek het en nie die vraag weer beantwoord het nie, merk die poging wat deurgetrek is.
- The mark for substitution is awarded for substitution into the correct formula.
Die punt vir substitusie word toegeken vir substitusie in die korrekte formule.

QUESTION 1/VRAAG 1

1.1.1	$\frac{1}{2}x^2 - x - 4 = 0$ $x^2 - 2x - 8 = 0$ $(x - 4)(x + 2) = 0$ $x = 4 \text{ or/of } x = -2$	✓✓ factors/faktore ✓ x-values/waardes (3)
1.1.2	$-3(x^2 + 3x) + 7 = 0$ $-3x^2 - 9x + 7 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-9) \pm \sqrt{(-9)^2 - 4(1)(7)}}{2(-3)}$ $x = 0,64 \text{ or/of } x = -3,64$	✓ standard form/standaardvorm ✓ substitution/substitusie ✓✓ x-values/waardes (4)
1.1.3	$2x^2 - 3x < 0$ $x(2x - 3) < 0$  $0 < x < \frac{3}{2}$	✓ x(2x - 3) ✓ critical values/kritiese waardes ✓✓ $0 < x < \frac{3}{2}$ (4)

QUESTION 2/VRAAG 2

2.1	$\frac{2x+2}{7x+1} = \frac{x-1}{2x+2}$ $(2x+2)^2 = (7x+1)(x-1)$ $4x^2 + 8x + 4 = 7x^2 - 6x - 1$ $3x^2 - 14x - 5 = 0$ $(3x+1)(x-5) = 0$ $x = -\frac{1}{3} \text{ or } x = 5$	$\checkmark \frac{T_2}{T_1} = \frac{T_3}{T_2}$ $\checkmark \text{standard form/standaardvorm}$ $\checkmark \text{factors/faktore}$ $\checkmark x = -\frac{1}{3}$ $\checkmark x = 5$
2.2	$25 ; 20 ; 16; \dots$ $a = 25 \quad ; \quad r = \frac{4}{5}$ $S_{\infty} = \frac{a}{1-r}$ $S_{\infty} = \frac{25}{1-\frac{4}{5}}$ $S_{\infty} = 125m$	$\checkmark r = \frac{4}{5}$ $\checkmark S_{\infty} = \frac{a}{1-r}$ $\checkmark \text{substitution/vervanging}$ $\checkmark S_{\infty} = 125m$
2.3	$a = 2$ $l = 29$ $S_n = 155$ $S_n = \frac{n}{2}(a+l)$ $155 = \frac{n}{2}(2+29)$ $n = 10$ $29 = 2 + (10-1)d$ $9d = 27$ $d = 3$	$\checkmark \text{sum formula of AS/ som formule van RR}$ $\checkmark \text{sub./vervanging van } a \text{ and/en } l$ $\checkmark n = 10$ $\checkmark \text{sub./vervanging van } n = 10$ $\checkmark d = 3$

QUESTION 3/VRAAG 3

3. $\begin{aligned} 2a &= 4 \\ a &= 2 \\ 24 &= 2 + b + c \quad \dots\dots\dots(1) \\ 24 &= 50 + 5b + c \quad \dots\dots\dots(2) \\ 4b &= -48 \qquad (2)-(1) \\ b &= -12 \\ 24 &= 2 - 12 + c \\ c &= 34 \\ T_n &= 2n^2 - 12n + 34 \end{aligned}$	$\checkmark 2a = 4$ $\checkmark a = 2$ \checkmark sub. into /vervang in T_1 \checkmark sub. into /vervang in T_5 \checkmark method of solving/metode van oplossing $\checkmark b = -12$ \checkmark sub. of /vervanging van b $\checkmark c = 34$
See alternative answers/ Kyk na alternatiewe antwoorde	(8) [8]

QUESTION 4/VRAAG 4

4.1	$36 = k^2$ $\therefore k = 6$	✓ sub of point/vervanging van punt ✓ $k = 6$ (2)
4.2	$y = 6^x$ $x = 6^y$ $y = \log_6 x$	✓ swop of x and y . / omruiling van x en y . ✓ $y = \log_6 x$ (2)
4.3	$0 < x \leq 1$	✓✓ answer/antwoord (2)
4.4	$y > 2$	✓✓ answer/antwoord (2) [8]

QUESTION 5/VRAAG 5

5.1	$B(5; 0)$	✓✓ answer /antwoord (2)
5.2	$y = a(x - p)^2 + q$ $y = a\left(x - \frac{3}{2}\right)^2 + \frac{49}{4}$ $0 = a\left(5 - \frac{3}{2}\right)^2 + \frac{49}{4}$ $a = -1$ $y = -1\left(x - \frac{3}{2}\right)^2 + \frac{49}{4}$ $y = -1\left(x^2 - 3x + \frac{9}{4}\right) + \frac{49}{4}$ $y = -x^2 + 3x + 10$ <p style="text-align: center;">OR/OF</p> $y = a(x - 5)(x + 2)$ Inspection/ <i>Inspeksie</i> $\frac{49}{4} = a\left(\frac{3}{2} - 5\right)\left(\frac{3}{2} + 2\right)$ $a = -1$ $y = -1(x - 5)(x + 2)$ $y = -x^2 + 3x + 10$	✓ sub of turning point/ vervanging van draaipunt ✓ sub of point B/ vervanging van punt B ✓ $a = -1$ ✓ $y = -x^2 + 3x + 10$ ✓ sub of x -intercepts/ vervanging van x -afsnitte ✓ sub of turning point/ vervanging van draaipunt ✓ $a = -1$ ✓ $y = -x^2 + 3x + 10$ (4)

5.3	$-x^2 + 3x + 10 = -x + 5$ $x^2 - 4x - 5 = 0$ $(x - 5)(x + 1) = 0$ $x = 5 \text{ or/of } x = -1$ $S(-1; 6)$	✓ $f(x) = g(x)$ ✓ standard form/ <i>standaardvorm</i> ✓ factors/faktore ✓ $S(-1; 6)$ (4)
5.4.1	$-1 \leq x \leq 5$	✓✓ answer/antwoord (2)
5.4.2	$-x^2 + 3x - 2,25 < 0$ $-x^2 + 3x + 10 < 2,25 + 10$ $\therefore f(x) < 12,25$ $x \in R ; x \neq 1,5$	✓ $f(x) < 12,25$ ✓✓ $x \in R ; x \neq 1,5$ accuracy/akkuraatheid (3) [15]

QUESTION 6/VRAAG 6

6.1		✓ asymptote/asimptoot ✓ x-intercept/x-afsnit ✓ shape/vorm ✓ other point/ander punt (4)
6.2	$f(x) = 2x^{-1} - 1$ $f'(x) = -2x^{-2}$	✓ $f'(x) = -2x^{-2} - 1$ ✓ $f'(x) = -2x^{-2}$ (2)
6.3	$h(x) = -x - 1$	✓✓ answer/antwoord (2)

<p>6.4</p> $f'(x) = -\frac{2}{x^2} \quad \text{and/en } h(x) = -x - 1$ $-\frac{2}{x^2} = -1$ $x^2 = 2$ $x = \sqrt{2}; \quad x > 0$ $f(\sqrt{2}) = \frac{2}{\sqrt{2}} - 1$ <p>Equation of tangent/vergelyking van raaklyn:</p> $y = -x + c$ $\frac{2}{\sqrt{2}} - 1 = -\sqrt{2} + c$ $c = -1 + 2\sqrt{2}$ $\therefore k = 2\sqrt{2}$	<ul style="list-style-type: none"> ✓ setting up of equation/ <i>opstel van vergelyking</i> ✓ $x = \sqrt{2}$ ✓ $\frac{2}{\sqrt{2}} - 1$ ✓ sub of $(\sqrt{2}; \frac{2}{\sqrt{2}} - 1)$/ <i>vervanging van</i> $(\sqrt{2}; \frac{2}{\sqrt{2}} - 1)$ ✓ $k = 2\sqrt{2}$
(5)	[13]

QUESTION 7/VRAAG 7

<p>7.1</p> $2000 \left(1 + \frac{8}{1200}\right)^{12} = 2000 \left(1 + \frac{r}{200}\right)^2$ $\sqrt{\left(1 + \frac{8}{1200}\right)^{12}} = \left(1 + \frac{r}{200}\right)$ $r = 8,13\%$	<ul style="list-style-type: none"> ✓ $\frac{8}{1200}$ and/en $\frac{r}{200}$ ✓ $n = 12$ and/en $n = 2$ ✓ $r = 8,13\%$
(3)	
<p>7.2</p> $A = P(1 - i)^n$ $4500 = 9500(1 - 7,7\%)^n$ $n = \frac{\log \frac{4500}{9500}}{\log(1 - 7,7\%)}$ $n \approx 9,325$ <p>It will take 10 years/Dit sal 10 jaar neem.</p>	<ul style="list-style-type: none"> ✓ correct formula/korrekte formule ✓ sub. of A and P/ vervanging van A en P ✓ use of logs/gebruik van logs ✓ $n \approx 9,325$ ✓ 10 years/10 jaar
(5)	
<p>7.3.1</p> $\frac{75}{100} \times 170\ 500 = R127\ 875$ <p style="text-align: center;">OR/ OF</p> $\frac{25}{100} \times 170\ 500 = 42\ 625$ $\text{Loan/lening} = 170\ 500 - 42\ 625$ $\text{Loan/lening} = R127\ 875$	<ul style="list-style-type: none"> ✓✓ answer/antwoord
(2)	OR/OF
<p>7.3.2</p> $127\ 875 = \frac{x \left[1 - \left(1 + \frac{13,2}{1200}\right)^{-60}\right]}{\frac{13,2}{1200}}$ $x = R\ 2\ 922,66$	<ul style="list-style-type: none"> ✓ $\frac{13,2}{1200}$ ✓ $n = 60$ ✓ sub of i, n and 127 875 into correct formula/ vervanging van i, n en 127 875 in die korrekte formule ✓✓ answer/antwoord
(5)	[15]

QUESTION 8/VRAAG 8

8.1	$f(x) = x - 2x^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{(x+h) - 2(x+h)^2 - (x - 2x^2)}{h}$ $= \lim_{h \rightarrow 0} \frac{(x+h) - 2(x^2 + 2xh + h^2) - x + 2x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{x + h - 2x^2 - 4xh - 2h^2 - x + 2x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{-4xh - 2h^2 + h}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-4x - 2h + 1)}{h}$ $= \lim_{h \rightarrow 0} (-4x - 2h + 1)$ $= -4x + 1$	<ul style="list-style-type: none"> ✓ formula/formule ✓ substitution of/substitusie van $(x + h)$ ✓ simplification/vereenvoudiging ✓ simplification to/ vereenvoudiging na $(-4xh - 2h^2 + h)$ ✓ common factor/gemene faktor ✓ answer/antwoord <p style="text-align: right;">(6)</p>
	<div style="border: 1px solid black; padding: 5px;"> Penalise 1 mark for incorrect use of formula. Must show $f'(x)$. <i>Penaliseer 1 punt vir verkeerde gebruik van formule. Moet $f'(x)$ toon.</i> </div>	
8.2.1	$y = \frac{1}{9}x^{-3} + 9x$ $\frac{dy}{dx} = -\frac{1}{3}x^{-4} + 9$	<ul style="list-style-type: none"> ✓ $-\frac{1}{3}x^{-4}$ ✓ 9 <p style="text-align: right;">(2)</p>
8.2.2	$y = -\frac{1}{2x\sqrt{x}} + x^3$ $y = -\frac{1}{2x \cdot x^{\frac{1}{2}}} + x^3$ $y = -\frac{1}{2}x^{-\frac{3}{2}} + x^3$ $\frac{dy}{dx} = \frac{3}{4}x^{-\frac{5}{4}} + 3x^2$	<ul style="list-style-type: none"> ✓ $\sqrt{x} = x^{\frac{1}{2}}$ ✓ $-\frac{1}{2}x^{-\frac{3}{2}}$ ✓ $\frac{3}{4}x^{-\frac{5}{4}}$ ✓ $3x^2$ <p style="text-align: right;">(4) [12]</p>

QUESTION 9/VRAAG 9

9.1	$h(x) = x^3 - 9x^2 + 23x - 15.$ $h'(x) = 3x^2 - 18x + 23$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-18) \pm \sqrt{(-18)^2 - 4(3)(23)}}{2(3)}$ $x = 4,15 \quad \text{or} \quad x = 1,85$ $x = 1,85 \text{ at C/by C}$	✓ $h'(x) = 3x^2 - 18x + 23$ ✓ sub into formula/ <i>vervang in formule</i> ✓ both x values/ <i>beide x waardes</i> ✓ $x = 1,85$ (4)	
9.2	$h(x) = x^3 - 9x^2 + 23x - 15.$ $h(x) = (x - 1)(x^2 - 8x + 15)$ $h(x) = (x - 1)(x - 3)(x - 5)$ $\therefore F(5; 0)$	✓ $(x - 1)(x^2 - 8x + 15)$ ✓ $(x - 1)(x - 3)(x - 5)$ ✓ ✓ $F(5; 0)$ (4)	
9.3	$h(x) = x^3 - 9x^2 + 23x - 15.$ $h'(x) = 3x^2 - 18x + 23$ $h''(x) = 6x - 18$ $6x - 18 = 0$ $x = 3$ $\therefore k = 3$	$x = \frac{4,15 + 1,85}{2}$ $x = \frac{6}{2}$ $x = 3$	✓ $h''(x) = 6x - 18$ ✓ $6x - 18 = 0$ ✓ $\therefore k = 3$ (3)
9.4	$h'(x) = 3x^2 - 18x + 23$ $h'(3) = 3(3)^2 - 18(3) + 23$ $h'(3) = -4$ $y = -4x + c$ $0 = -4(3) + c$ $c = 12$ $y = -4x + 12$	✓ $h'(3) = -4$ ✓ sub of point D/ <i>vervanging van punt D</i> ✓ $y = -4x + 12$ (3) [14]	

QUESTION 10/VRAAG 10

10.1	$P = x \left(50 - \frac{1}{2}x \right) - \left(\frac{1}{4}x^2 + 35x + 25 \right)$ $P = 50x - \frac{1}{2}x^2 - \frac{1}{4}x^2 - 35x - 25$ $P = -\frac{3}{4}x^2 + 15x - 25$	✓ $x \left(50 - \frac{1}{2}x \right)$ ✓ subtracting total cost/ <i>aftrekking van totale koste</i> (2)
10.2	$\frac{dP}{dx} = -\frac{3}{2}x + 15$ $-\frac{3}{2}x + 15 = 0$ $x = 10$	✓ $\frac{dP}{dx} = -\frac{3}{2}x + 15$ ✓ $-\frac{3}{2}x + 15 = 0$ ✓ $x = 10$ (3)
10.3	$C = \frac{\frac{1}{4}x^2 + 35x + 25}{x}$ $C = \frac{1}{4}x + 35 + 25x^{-1}$ $\frac{dC}{dx} = \frac{1}{4} - 25x^{-2}$ $\frac{1}{4} - 25x^{-2} = 0$ $\frac{25}{x^2} = \frac{1}{4}$ $x^2 = 100$ $x = 10$ <p>∴ Minimum /Minimum</p>	✓ $C = \frac{\frac{1}{4}x^2 + 35x + 25}{x}$ ✓ $C = \frac{1}{4}x + 35 + 25x^{-1}$ ✓ $\frac{dC}{dx} = \frac{1}{4} - 25x^{-2}$ ✓ $\frac{1}{4} - 25x^{-2} = 0$ ✓ $x = 10$ (5) [10]

QUESTION 11/VRAAG 11

11.1.1	$P(M) = \frac{1200}{1600}$ $P(M) = \frac{3}{4}$ or/of 0,75	✓ answer/antwoord (1)
11.1.2	$P(Fail) = \frac{200}{1600}$ $P(Fail) = \frac{1}{8}$	✓ answer/antwoord (1)
11.1.3	$P(M) \times P(F) = \frac{3}{4} \times \frac{1}{8}$ $= \frac{3}{32}$ $\frac{3}{32} = \frac{A}{1600}$ $A = 150$	✓ $\frac{3}{4} \times \frac{1}{8}$ ✓ $\frac{3}{32}$ ✓ $\frac{3}{32} = \frac{A}{1600}$ (3)
11.1.4	$B = 1050$ $C = 50$ $D = 350$	✓ $B = 1050$ ✓ $C = 50$ ✓ $D = 350$ (3)
11.1.5	$P(F/F) = \frac{50}{1600}$ $P(F/F) = \frac{1}{32}$	✓ 50 ✓ 1600 (2)
11.2.1	$9! = 362880$	✓✓ answer/antwoord (2)
11.2.2	$4! \times 5! \times 6$ $= 17 280$ OR/OF $6! \times 4! = 17280$	✓ $4! \times 5!$ ✓ $\times 6$ ✓ 17280 (3) [15]

TOTAL/TOTAAL: 150

ALTERNATIVE ANSWERS / ALTERNATIEWE ANTWOORDE

<p>1.1.1</p> $\frac{1}{2}x^2 - x - 4 = 0$ $\left(\frac{1}{2}x + 1\right)(x - 4) = 0$ $x = -2 \text{ or/of } x = 4$ <p style="text-align: center;">OR/OF</p> $\frac{1}{2}x^2 - x - 4 = 0$ $\left(\frac{1}{2}x - 2\right)(x + 2) = 0$ $x = 4 \text{ or/of } x = -2$ <p style="text-align: center;">OR/OF</p> $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4\left(\frac{1}{2}\right)(-4)}}{2\left(\frac{1}{2}\right)}$ $x = 4 \text{ or/of } x = -2$	<p>✓✓ factors/faktore ✓ x-values/waardes (3)</p> <p>✓✓ factors/faktore ✓ x-values/waardes (3)</p> <p>✓✓ sub into formula/vervang in formule ✓ x-values/waardes</p>
<p>3.1</p> $2a = 4$ $a = 2$ $T_3 = \text{axis of symmetry /simmetriese as}$ $T_n = a(n + p)^2 + q$ $T_n = 2(n + p)^2 + q$ $T_n = 2(n - 3)^2 + q$ $24 = 2(1 - 3)^2 + q$ $q = 16$ $T_n = 2(n - 3)^2 + 16$ $T_n = 2(n^2 - 6n + 9) + 16$ $T_n = 2n^2 - 12n + 34$	<p>✓ $2a = 4$ ✓ $a = 2$ ✓ $T_n = 2(n + p)^2 + q$ ✓ $T_n = 2(n - 3)^2 + q$ ✓ $24 = 2(1 - 3)^2 + q$ ✓ $q = 16$ ✓ $T_n = 2(n^2 - 6n + 9) + 16$ ✓ $T_n = 2n^2 - 12n + 34$ (8)</p>
<p>5.4.2</p> $-x^2 + 3x - \frac{9}{4} < 0$ $x^2 - 3x + \frac{9}{4} > 0$ $4x^2 - 12x + 9 > 0$ $(2x - 3)(2x - 3) > 0$ $\therefore x \in R ; x \neq \frac{3}{2}$	<p>✓ factors/faktore ✓✓ answer/antwoord (3)</p>