



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE /
NASIONALE
SENIOR SERTIFIKAAT**

GRADE/GRAAD 12

JUNE/JUNIE 2019

**TECHNICAL MATHEMATICS P1/TEGNIESE WISKUNDE V1
MARKING GUIDELINE/NASIENRIGLYN**

MARKS/PUNTE: 150

Marking Codes/Nasienkodes	
A	Accuracy / Akkuraatheid
CA	Consistent accuracy / Deurlopende akkuraatheid
M	Method / Metode
R	Rounding / Ronding
NPR	No penalty for rounding / Geen penalisering vir ronding
NPU	No penalty for units omitted / Geen penalisering vir geen eenhede
S	Simplification / Vereenvoudiging
SF	Substitution in the correct formula / Vervanging in 'n korrekte formule

This marking guideline consists of 15 pages./
Hierdie nasienriglyn bestaan uit 15 bladsye.

NOTE/LET WEL:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- *Indien 'n kandidaat 'n vraag TWEE keer beantwoord, sien slegs die EERSTE poging na.*
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed-out version.
- *Indien 'n kandidaat 'n poging gekanselleer het, maar dit nie weer gedoen het nie, sien die gekanselleerde poging na.*
- Consistent accuracy (CA) applies to ALL aspects of the marking guideline.
- *Volgehoue akkuraatheid (CA) is deurgaans in ALLE aspekte van die nasienriglyn van toepassing.*
- Assuming answers/values to solve a problem is NOT acceptable.
- *Aanvaarding van waardes/antwoorde om 'n probleem op te los, is onaanvaarbaar.*

QUESTION/VRAAG 1				
1.1	1.1.1	$(7x-1)(x+2) = 0$ $7x-1=0$ or $x+2=0$ $\therefore x = \frac{1}{7}$ or/of $x = -2$	$\checkmark x = \frac{1}{7}$ $\checkmark x = -2$	A A (2)
	1.1.2	$(x-2)(3x-1) = 1$ $3x^2 - 7x + 1 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(3)(1)}}{2(3)}$ $x = 2,18$ or/of $x = 0,15$	<div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> -1 MARK for incorrect rounding/ -1 PUNT vir verkeerde afronding </div> \checkmark Simplification/Standard Form/Vereenvoudiging/ Standaardvorm A \checkmark Formula/Formule A \checkmark Substitution/Vervanging CA \checkmark Both values of x /Beide waardes van x CA R	(4)
	1.1.3	$-x^2 - 4x + 5 \geq 0$ $x^2 + 4x - 5 \leq 0$ $(x+5)(x-1) \leq 0$ C.V: -5 and 1 Solution: $-5 \leq x \leq 1$ OR / OF $x \in [-5; 1]$ OR / OF $x \geq -5$ and / en $x \leq 1$	\checkmark Factors/ Substitution in the quadratic formula M A <i>Faktore/Vervanging in kwadratiese formule</i> \checkmark Critical Values/ Kritiese waardes CA NPR \checkmark Correct Notation CA <i>Korrekte notasie</i>	(3)

1.2	<p>Total thickness of the pack/ = $151 \div 1\,000 = 0,151$ m <i>Totale dikte van die bondel</i></p> <p>Thickness of 1 metal sheet = $0,151 \div 300$ <i>Dikte van 1 metaalblad</i></p> $= \frac{151}{300000}$ $= 5,03 \times 10^{-4} \text{ m}$ <p style="text-align: center;">OR/OF</p> <p>Thickness of one metal sheet = $\left(\frac{151}{300}\right) \div 1000$ $= 5,03 \times 10^{-4} \text{ m}$</p>		<p>✓Conversion/<i>Herleiding</i> A</p> <p>✓Method/<i>Metode</i> CA M</p> <p>✓$5,03 \times 10^{-4}$ CA NPU</p>	(3)
1.3	1.3.1	$(y - 5x)(y + 5x)$	<p>✓Factors/<i>Faktore</i> A</p>	(1)
	1.3.2	<p>$2y + 6x = 4$ and / <i>en</i> $y^2 - 25x^2 = 4$ $y = -3x + 2$ substitute y into $y^2 - 25x^2 = 4$</p> $(-3x + 2)^2 - 25x^2 - 4 = 0$ $9x^2 - 12x + 4 - 25x^2 - 4 = 0$ $-16x^2 - 12x = 0$ $-x(16x + 12) = 0$ $x = 0 \text{ or / en } 16x = -12$ $x = 0 \text{ or / en } x = -\frac{12}{16} = -\frac{3}{4}$ <p>if $x = 0$ then / <i>dan</i> $y = 2$ if $x = -\frac{3}{4}$ then / <i>dan</i> $y = -3\left(-\frac{3}{4}\right) + 2$ $= \frac{17}{4}$</p>	<p>✓y - the subject/<i>die onderwerp</i> A</p> <p>✓Substitution by/<i>Vervang deur</i> $y = -3x + 2$ SF CA</p> <p>✓Simplification/<i>Vereenvoudig</i> Standard form/ <i>Standaardvorm</i> S CA</p> <p>✓Factors/<i>Faktore</i> CA</p> <p>✓x-values/<i>waardes</i> CA</p> <p>✓y-values/<i>waardes</i> CA</p>	(6)

	1.3.2	<p style="text-align: center;">OR/OF</p> <p>Substitute/<i>Vervang</i> $y = -3x + 2$ into/<i>in</i> $(y - 5x)(y + 5x) = 4$ $(-3x + 2 - 5x)(-3x + 2 + 5x) = 4$ $(-8x + 2)(2x + 2) = 4$ $-1 - 16x^2 - 12x + 4 - 4 = 0$ $-16x^2 - 12x = 0$ $-x(16x + 12) = 0$ $x = 0$ or / <i>of</i> $16x = -12$ $x = 0$ or / <i>of</i> $x = -\frac{12}{16} = -\frac{3}{4}$ if $x = 0$ then / <i>dan</i> $y = 2$ if $x = -\frac{3}{4}$ then / <i>dan</i> $y = -3\left(-\frac{3}{4}\right) + 2$ $= \frac{17}{4}$</p>	<p>✓ y - the subject/<i>-die onderwerp</i> A</p> <p>✓ Substitution by/<i>Vervang deur</i> $y = -3x + 2$ SF CA</p> <p>✓ Simplification/Standard form <i>Vereenvoudig/Standaardvorm</i> S CA</p> <p>✓ Factors/<i>Faktore</i> CA</p> <p>✓ x-values/<i>waardes</i> CA</p> <p>✓ y-values/<i>waardes</i> CA</p>																									
1.4	1.4.1	$p \in \{1; 2; 3; 4; 5\}$	<p>✓✓ All 5 correct values/ <i>Al 5 korrekte waardes</i> A</p> <p>✓ Only 3 correct values/ <i>Slegs 3 korrekte waardes</i> A No mark for less than 3 values <i>Geen punt vir minder as 3 waardes</i></p>	(2)																								
	1.4.2	$p = 6$	<p>✓ 6 A</p>	(1)																								
1.5	Real, rational and unequal/ <i>Reël, rasionaal en ongelyk</i>		<p>✓ Real and unequal/<i>Reël en ongelyk</i> A</p> <p>✓ Rational/<i>Rasionaal</i> A</p>	(2)																								
1.6	$86 = 2^6 + 2^4 + 2^2 + 2^1$ $= 1010110_2$ OR/OF	<table border="1" data-bbox="240 1697 627 2002"> <thead> <tr> <th>2</th> <th>86</th> <th>Remainder/Res</th> </tr> </thead> <tbody> <tr><td>2</td><td>43</td><td>0</td></tr> <tr><td>2</td><td>21</td><td>1</td></tr> <tr><td>2</td><td>10</td><td>1</td></tr> <tr><td>2</td><td>5</td><td>0</td></tr> <tr><td>2</td><td>2</td><td>1</td></tr> <tr><td>2</td><td>1</td><td>0</td></tr> <tr><td></td><td>0</td><td>1</td></tr> </tbody> </table> <div data-bbox="655 1630 943 1798" style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p style="text-align: center;">-1 Mark of base 2 is not written -1 Punt vir basis 2 nie geskryf nie</p> </div>	2	86	Remainder/Res	2	43	0	2	21	1	2	10	1	2	5	0	2	2	1	2	1	0		0	1	<p>✓ Method/<i>Metode</i> M</p> <p>✓ Accurate answer/<i>Akkurate antwoord</i> A</p>	(2)
2	86	Remainder/Res																										
2	43	0																										
2	21	1																										
2	10	1																										
2	5	0																										
2	2	1																										
2	1	0																										
	0	1																										
				[26]																								

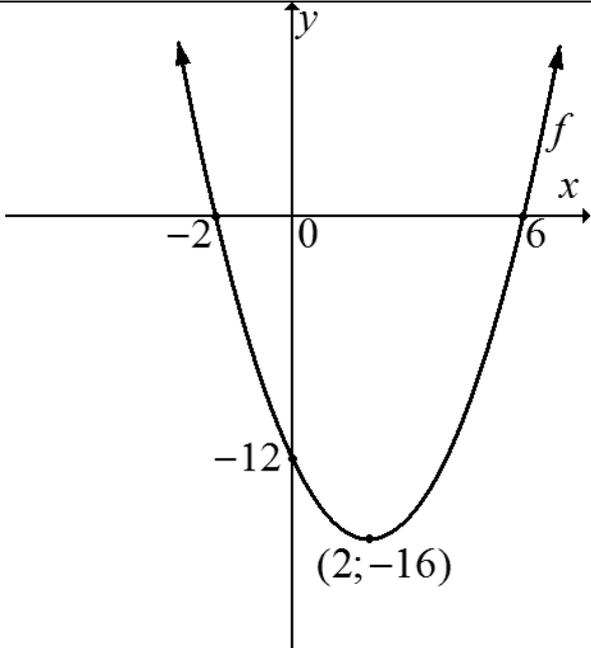
QUESTION/VRAAG 2				
2.1	2.1.1	$3^n \cdot 3^4 = 3^{n+4}$	$\checkmark 3^{n+4}$	A (1)
	2.1.2	$\frac{7 \cdot 3^{n+2}}{3^{n+4} - 6 \cdot 3^{n+1}}$ $= \frac{3^n \cdot 3^2 \cdot 7}{3^n (3^4 - 6 \cdot 3)}$ $= \frac{63}{63}$ $= 1$	\checkmark Factors/ <i>Faktore</i> S \checkmark Simplification/ <i>Vereenvoudig</i> S CA	(2)
	2.1.3	$\sqrt{32} - \sqrt{72} + \sqrt{18}$ $= 4\sqrt{2} - 6\sqrt{2} + 3\sqrt{2}$ $= \sqrt{2}$	\checkmark Simplification/ <i>Vereenvoudig</i> S \checkmark Simplification/ <i>Vereenvoudig</i> S CA	(2)
	2.1.4	$-\log_3 243 + \log_3 1$ $= -\log_3 3^5 + 0$ $= -5$	$\checkmark 0$ A $\checkmark -5$ S CA	(2)
2.2	2.2.1	$\frac{(4^x)^{2x} \cdot \sqrt{16^{-3}}}{4^x} = (4^x)^0$ $\frac{(4^{2x^2}) \cdot 4^{2x \cdot \frac{-3}{2}}}{4^x} = 4^0$ $4^{2x^2 - 3 - x} = 4^0$ $2x^2 - x - 3 = 0$ $(2x - 3)(x + 1) = 0$ $x = \frac{3}{2} \text{ or/of } x = -1$	\checkmark Power rule/ <i>Magreël</i> A \checkmark Same base/ <i>Dieselfde basis</i> S CA \checkmark Equal exponents/ <i>Gelyke eksponente</i> CA \checkmark Factors/ <i>Faktore</i> S M CA $\checkmark x = \frac{3}{2}$ CA $\checkmark x = -1$ CA	(6)

2.2.2	$x = \frac{\log 6 - \log 2}{\log 9(2 \log 5 + \log 4)}$ $x = \frac{\log \frac{6}{2}}{\log 9(\log 100)}$ $x = \frac{\log 3}{2 \times 2 \log 3}$ $x = \frac{1}{4}$ <p style="text-align: center;">OR/OF</p> $x = \frac{\log 6 - \log 2}{\log 9(2 \log 5 + \log 4)}$ $x = \frac{\log 3 + \log 2 - \log 2}{\log 9(\log 100)}$ $x = \frac{\log 3}{2 \times 2 \log 3}$ $x = \frac{1}{4}$	<p>✓Log law/wet A</p> <p>✓Log law/wet A</p> <p>✓Simplification/ Vereenvoudig S CA</p> <p>✓$x = \frac{1}{4}$ CA</p> <p>✓Log law/wet A</p> <p>✓Log law/wet A</p> <p>✓Simplification/ Vereenvoudig S CA</p> <p>✓$x = \frac{1}{4}$ CA</p>	(4)
2.3	$x + 2yi = (-2 + 6i)(4 - 7i)$ $= -8 + 14i + 24i - 42i^2$ $= -8 + 38i + 42$ $= 34 + 38i$ $x = 34 \text{ and/en } 2y = 38$ $y = 19$	<p>✓Expansion/Uitbreiding S</p> <p>✓$i^2 = -1$ A</p> <p>✓x-value/waardes CA</p> <p>✓y-value/waardes CA</p>	(4)
2.4	$z = \sqrt{5} - 3i$ $r = \sqrt{(\sqrt{5})^2 + (-3)^2}$ $= \sqrt{14}$ $= 3,74$ $\tan \theta = -\frac{3}{\sqrt{5}}$ $\theta = -53,3^\circ \text{ or/of } \theta = 360^\circ - 53,3^\circ = 306,7^\circ$ $z = 3,74 \text{ cis } 306,7^\circ$	<p>✓Finding/Vind r SF</p> <p>✓$r = \sqrt{14} / 3,74$ S CA</p> <p>✓$\tan \theta = -\frac{3}{\sqrt{5}}$ A</p> <p>✓$\theta = -53,3^\circ$ CA</p> <p>✓$z = \sqrt{14} \text{ cis } 306,7^\circ /$ $z = 3,74 \text{ cis } 306,7^\circ$ CA</p>	(5)
			[26]

QUESTION/VRAAG 3			
3.1	$x = 0$ and/en $y = 0$	$\checkmark x = 0$ $\checkmark y = 0$	A A (2)
3.2	$y = 1$	$\checkmark y = 1$	A (1)
3.3		\checkmark Shape/Vorm g \checkmark y -intercept of g / y -afsnit van g \checkmark Shape/Vorm h	A CA A (3)
3.4	$x \neq 0, x \in R$	$\checkmark x \neq 0, x \in R$	CA (1)
3.5	$x < -1$ or / of $x > 0$ OR/OF $x \in (-\infty; -1)$ or / of $x \in (0; \infty)$ OR/OF $-\infty < x < -1$ or / of $0 < x < \infty$	$\checkmark x < -1$ \checkmark or / of $x > 0$	CA CA (2)
			[9]

QUESTION/VRAAG 4			
4.1	$r = \sqrt{(-3)^2 + (-3)^2} = \sqrt{18}$ $y = -\sqrt{18-x^2}$	✓ Value of/waarde van r SF ✓ Accurate equation of h / <i>Akkurate vergelyking van h</i> A	(2)
4.2	$m = \frac{-3}{-3} = 1$ $m_{\text{tangent}} = -1$ substitute / vervang $P(-3; -3)$ into / in $y = mx + c$ $-3 = -(-3) + c$ $-6 = c$ Equation of the tangent / <i>Vergelyking van die raaklyn</i> is $y = -x - 6$	✓ m of the line through origin and P / m van die lyn deur oorsprong P A ✓ m tangent/raaklyn CA ✓ Substitution by P / <i>Vervanging van P</i> SF CA ✓ Equation of the tangent in the form $y =$ / <i>Vergelyking van die raaklyn in die vorm van $y =$</i> CA	(4)
4.3	$y : -\sqrt{18} \leq y \leq 0 \text{ OR / OF } y \in [-\sqrt{18}; 0]$ $\text{OR / OF } y \geq -\sqrt{18} \text{ and / en } y \leq 0$	✓✓ Accurate answer/ <i>Akkurate antwoord</i> A	(2)
			[8]

QUESTION/VRAAG 5			
5.1	$f(x) = ax^2 + bx - 12$ $= a(x+2)(x-6)$ $= a(4x^2 - 4x - 12)$ $= 4ax^2 - 4ax - 12a$ <p>then / dan $-12a = -12$</p> $a = 1$ $b = -4(1) = -4$ <p style="text-align: center;">OR/OF</p> $f(-2) = a(-2)^2 + b(-2) - 12 = 0$ $= 4a - 2b - 12 = 0$ $f(6) = a(6)^2 + b(6) - 12 = 0$ $= 36a + 6b - 12 = 0$ $3(4a - 2b - 12) = 0$ $12a - 6b - 36 = 0 \dots\dots\dots 1$ $36a + 6b - 12 = 0 \dots\dots\dots 2$ <p>by elimination / deur eliminasie :</p> $48a - 48 = 0$ $a = 1$ <p>then / dan, $12(1) - 6b - 36 = 0$</p> $-6b = 36 - 12$ $b = -4$	<p>✓Substitution/Vervanging SF</p> <p>✓Simplification/Vereenvoudig S</p> <p>✓Method for a/Metode van a M</p> <p>✓Method for b/Metode van b M</p>	(4)
5.2	$f(x) = x^2 - 4x - 12$ $x = \frac{-b}{2a} = -\frac{(-4)}{2(1)} = 2$ $f(2) = 2^2 - 4(2) - 12 = -16$ <p>T.P(2; -16)</p> <p style="text-align: center;">OR / OF</p> $f'(x) = 2x - 4 = 0$ $x = 2$ $f(2) = 2^2 - 4(2) - 12 = -16$ <p>TP(2; -16)</p> <p style="text-align: center;">OR / OF</p> $x = \frac{x_1 + x_2}{2} = \left(\frac{-2 + 6}{2} \right) = 2$ $f(2) = 2^2 - 4(2) - 12 = -16$ <p>TP(2; -16)</p>	<p>✓Method/Metode M</p> <p>✓$x = 2$ CA</p> <p>✓$y = -16$ CA</p>	(3)

5.3		<ul style="list-style-type: none"> ✓ <i>x</i>-intercepts/<i>x</i>-afsnit A ✓ <i>y</i>-intercept/<i>y</i>-afsnit A ✓ Turning point/<i>Draaipunt</i> CA ✓ Shape/<i>Vorm</i> A 	
			(4)
			[11]

QUESTION/VRAAG 7				
NOTE : Deduct 1 mark for incorrect notation from 7.1 to 7.2.2				
LET WEL: Trek 1 punt af vir inkorrekte notasie van 7.1 tot 7.2.2				
7.1		$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{[5(x+h) - 12] - (5x - 12)}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{5x + 5h - 12 - 5x + 12}{h}$ $f'(x) = \lim_{h \rightarrow 0} \frac{5h}{h}$ $= \lim_{h \rightarrow 0} 5$ $= 5$	✓Formula/Formule A ✓Substitution/Vervanging SF ✓Simplification/Vereenvoudig S CA ✓Simplification/Vereenvoudig S CA ✓ $f'(x) = 5$ CA	(5)
7.2	7.2.1	$D_x \left(3\pi + \frac{2}{x^2} - 5x^3 \right)$ $= D_x (3\pi + 2x^{-2} - 5x^3)$ $= 0 - 4x^{-3} - 15x^2$	✓ $2x^{-2}$ A ✓ 0 A ✓ $-4x^{-3}$ CA ✓ $-15x^2$ A	(4)
	7.2.2	$y = 11x^{-3} + \frac{2}{5}x^{\frac{1}{5}} + \sqrt{x^2}$ $y = 11x^{-3} + \frac{2}{5}x^{\frac{1}{5}} + x$ $\frac{dy}{dx} = -33x^{-4} + \frac{2}{25}x^{-\frac{4}{5}} + 1$	✓ x A ✓ $-33x^{-4}$ A ✓ $\frac{2}{25}x^{-\frac{4}{5}}$ A ✓ 1 CA	(4)

7.3	7.3.1	$h(x) = 3x^2 - 7x + 2$ $h'(x) = 6x - 7$ $h'(0,5) = 6(0,5) - 7$ $m_{\text{tangent}} = -4$ $m_{\text{raaklyn}} = -4$	$\checkmark 6x - 7$ \checkmark Substitution/Vervanging $\checkmark m_{\text{tangent}} = -4$ $m_{\text{raaklyn}} = -4$	A SF CA CA	(3)
	7.3.2	$h(x) = 3x^2 - 7x + 2$ $h(1) = 3(1)^2 - 7(1) + 2 = -2$ $h(3) = 3(3)^2 - 7(3) + 2 = 8$ Av.gradient / Gem. gradiënt = $\frac{h(3) - h(1)}{3 - 1}$ $= \frac{8 + 2}{3 - 1}$ $= 5$	$\checkmark -2$ $\checkmark 8$ \checkmark Correct substitution/ Korrekte vervanging \checkmark Simplification / Vereenvoudiging	A A SF CA S CA	(4)
					[20]
QUESTION/VRAAG 8					
8.1		$g(x) = x^3 - x$ $0 = x(x^2 - 1)$ $0 = x(x - 1)(x + 1)$ $x = 0$ or/of $x = 1$ or/of $x = -1$ A(-1;0) B(1;0)	\checkmark Substitution by 0/ Vervanging deur 0 \checkmark Factors/Faktore \checkmark Coordinates of A/ Koördinate van A \checkmark Coordinates of B/ Koördinate van B	SF S CA CA	(4)
8.2		$f(x) = x^3 - x$ $f'(x) = 3x^2 - 1$ $0 = 3x^2 - 1$ $\frac{1}{3} = x^2$ $x = \pm \sqrt{\frac{1}{3}}$ or/of $\pm 0,58$ $g(0,58) = (0,58)^3 - 0,577 = -0,38$ $g(-0,58) = (-0,58)^3 - (-0,58) = 0,38$ K(-0,58;0,38) M(0,58;-0,38)	\checkmark Derivative/Afgelei $\checkmark 0$ \checkmark Both x values/Beide waardes van x \checkmark y-coordinate of K/ Koördinate van K \checkmark y-coordinate of M/ Koördinate van M	A A CA CA	(5)
8.3		$-0,58 \leq x \leq 0,58$	$\checkmark -0,58$ $\checkmark 0,58$ \checkmark Correct notation/Korrekte notasie	CA CA A	(3)
					[12]

QUESTION/VRAAG 10				
10.1		$\int \frac{2x^8 + x^5 - 13x^2}{x^3} dx$ $\int 2x^5 + x^2 - \frac{13}{x} dx$ $= \frac{1}{3}x^6 + \frac{1}{3}x^3 - 13 \ln x + c$	<p>✓Simplification/Vereenvoudig A</p> <p>✓$\frac{1}{3}x^6$ CA</p> <p>✓$\frac{1}{3}x^3$ CA</p> <p>✓$-13 \ln x$ CA</p> <p>✓c A</p>	(5)
10.2	10.2.1	$\int -x^3 + 6x^2 dx$ $= -\frac{x^4}{4} + 2x^3 + c$	<p>✓$-\frac{x^4}{4}$ A</p> <p>✓$2x^3$ A</p> <p>✓c A</p>	(3)
	10.2.2	$ A = \int_1^4 -x^3 + 6x^2 dx$ $= \left[-\frac{x^4}{4} + 2x^3 \right]_1^4$ $= \left(-\frac{(4)^4}{4} + 2(4)^3 \right) - \left(-\frac{(1)^4}{4} + 2(1)^3 \right)$ $ A = 64 - 1,75$ $= 62,25 \text{ square units}$ <p><i>kwadratiese eenhede</i></p>	<p>✓A definite integral formula <i>'n Definitiewe intergrale formule</i> A</p> <p>✓Simplification/Vereenvoudig S</p> <p>✓Substitution in A by 4/ <i>Vervanging in A deur 4</i> SF CA</p> <p>✓Substitution in A by 1/ <i>Vervanging in A deur 1</i> SF CA</p> <p>✓Simplification/Vereenvoudig CA</p>	(5)
				[13]
			TOTAL/TOTAAL:	150

